

## SIMULATION OF SIMULTANEOUS LOCALIZATION AND MAPPING BASED ON THE UNSCENTED KALMAN FILTER FOR SMALL UNMANNED UNDERWATER VEHICLES

**Arom Hwang**

Department of Naval Architecture and Ocean Engineering, Koje College,  
Majeon 1 gil 91, Goeje, Gyeongsangnam-do, Korea

**Abstract** — This paper proposes a simultaneous localization and mapping (SLAM) scheme that is applicable to the autonomous navigation of unmanned underwater vehicles (UUVs). A SLAM scheme is an alternative navigation method for measuring the environment through which the vehicle is passing and providing the relative position of the UUV. An unscented Kalman filter (UKF) is utilized to develop a SLAM that is suitable to estimate the locations of the UUV and the surrounding objects when the motion of the UUV is highly nonlinear. A range sonar is used as a sensor to collect the data including the spatial information of the environment in which the UUV is navigating. The proposed UKF-SLAM scheme was validated through simulations and experiments that used various two and three degrees of freedom motion conditions with a real UUV in a towing tank environment. The results of these simulations and experiments showed that the proposed SLAM algorithm is capable of estimating the position of the UUV and the surrounding objects under highly nonlinear motion and demonstrated that the algorithm can perform well in various conditions.

**Key words** — Simultaneous localization and mapping (SLAM), range sonar, unmanned underwater vehicle (UUV), unscented Kalman filter (UKF), towing tank simulation.

### Introduction

During the last decade, the use of unmanned underwater vehicles (UUVs) has been increasing in various areas of underwater survey operations in scientific, military, and commercial applications due to its autonomy and extended operation time capabilities (Chyba, 2009); the use of these vehicles has also extended to the inspection of ship hulls (Walter *et al.*, 2008) and underwater man-made structures (Kondo *et al.*, 2006; Ribas *et al.*, 2008) due to the UUV ability of autonomous navigation. Since GPS signal is not accessible underwater, the position of the UUV has usually been estimated via dead reckoning using an inertia measurement unit (IMU) and a kinematics model for vehicle motion. However, the method based dead reckoning is disadvantageous in that the navigation error becomes unbounded as the navigation time elapses due to the drift produced when integrating the IMU's output; thus, it is necessary to provide some additional measures to prevent further error accumulation so that the ground fixed relative positioning information can be obtained (Lee *et al.*, 2005). One of the alternative approaches that has been suggested to overcome the demerits of dead reckoning is a method that uses measured environmental data from the area through which the vehicle is passing; for example, it is possible to use the range and angle of identified objects that

exist in the operating area as sources of information for a ground fixed relative position (Smith *et al.*, 1997). Simultaneous localization and mapping (SLAM) is one technique that is used to measure data for navigation. SLAM is designed to simultaneously identify distinct objects in an unknown environment where a prior map is not available and then it can utilize this information to localize the trajectory of the vehicle (Smith *et al.*, 1990).

Since stochastic mapping, which is the basis of SLAM, is an estimation process, all estimation methods can be implemented into SLAM. Although any estimation method can be used in SLAM, many studies have applied an extended Kalman filter (EKF) to SLAM for indoor ground vehicles (Tardos *et al.*, 2002), outdoor ground vehicles (Dissanyake *et al.*, 2001), and underwater vehicles (Smith *et al.*, 1997; Carpenter, 1998; Newman, 1999; Leonard and Feder, 2001; Hwang and Seong, 2005; Folkesson *et al.*, 2008; Ribas *et al.*, 2008) because EKF is considered optimal when assumptions that the system is locally linear and the probability density function (PDF) is a Gaussian distribution are satisfied (Welch and Bishop, 2006). However, if a nonlinear system cannot satisfy the locally linear assumption, the result estimated by the EKF for the nonlinear system might yield a divergence; thus, it is not appropriate to apply EKF to SLAM for highly nonlinear systems. One of the alternatives to a SLAM based EKF is a SLAM with an unscented Kalman filter (UKF). A UKF (Julier and Uhlmann, 1997, 2004) not only estimates the mean and covariance of the nonlinear system, as EKF does, but also obtains the transformed PDF from the weighted sum of the evaluation of the nonlinear system equation at samples of prior PDF, called sigma points, instead of the Jacobian matrix of the nonlinear system equation.

Up to now, since the UKF can produce a consistent unbiased estimate even when the system is highly nonlinear, recent studies have attempted to implement UKF into SLAM for unmanned land vehicles (Lee *et al.*, 2006; Andrade-Cetto *et al.*, 2005) and unmanned aerial vehicles (Langelaan and Rock, 2005), and to verify the SLAM with the UKF through simulations and experiments. However, although the motion of UUVs is usually nonlinear, there are few studies on SLAM with UKF for UUVs. Thus, a SLAM based on the UKF for UUVs will be proposed in this work and will be verified through simulations in tank conditions.

This paper proceeds as follows. Section 2 describes the SLAM based on the UKF that is suitable for UUVs with a range sonar system. Section 3 presents the results of the simulations in tank conditions, conducted to verify the proposed SLAM method. Section 4 concludes the paper.

## Simultaneous localization and mapping formulation with unscented Kalman filter

### A. State model

Consider the SLAM problem in which a UUV is navigating in the ocean with multiple objects located adjacent to where the vehicle is operating. If the UUV is assumed to move in three degrees of freedom, the state of the vehicle can be written as:

$$\mathbf{x}_v = [x_v \quad y_v \quad \psi_v \quad \theta_v \quad V_v]^T, \quad (1)$$

where denote the position in a three dimensional space; denote the heading and pitch angle, respectively, and denotes the total velocity. As the motion of the UUV is assumed to be divided into two planes, vertical and horizontal planes in this work, only surge, yaw, and pitch are considered in (1).

The state of  $M$  objects acquired by the sensor on the UUV is given by their positions:

$$\mathbf{x}_o = [x_{o1} \ y_{o1} \ z_{o1} \ \cdots \ x_{oM} \ y_{oM} \ z_{oM}]^T. \quad (2)$$

The objects' positions are assumed to be fixed and unassociated with each other.

Since the system state vector in SLAM is defined as the combination of a vehicle state and an object's state, the system state vector in this work is as follows:

$$\mathbf{x} = [\mathbf{x}_v^T \ \mathbf{x}_o^T]^T. \quad (3)$$

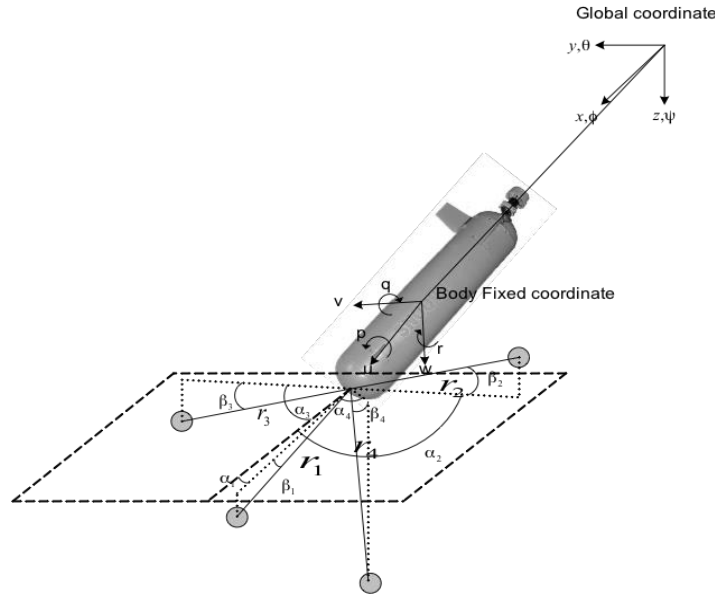
In this work, the vehicle motion is modeled with a second kinematics model, which is characterized by a constant velocity with white noise acceleration (Bar-Shalom and Forman, 1988). The discrete time state equation at time  $k$  and  $k+1$  with sampling time is described as:

$$\begin{aligned} x_v(k+1) &= x_v(k) + V_v \cos(\theta_v + r) \cos(\theta_v + q) \Delta T + q_x(k) y_v(k+1) \\ y_v(k) &+ V_v \sin(\theta_v + r) \cos(\theta_v + q) \Delta T + q_y(k) z_v(k+1) \\ z_v(k) &+ V_v \sin(\theta_v + q) \Delta T + q_z(k) \\ \psi_v(k+1) &= \psi_v(k) + r + q_\psi(k) \\ \theta_v(k+1) &= \theta_v(k) + q + q_\theta(k) \\ V_v(k+1) &= V_v(k) + q_v(k) \\ \mathbf{x}_o(k+1) &= \mathbf{x}_o(k), \end{aligned} \quad (4)$$

where  $q_x, q_y, q_z, q_\psi, q_\theta, q_v$  are the process noises.

#### B. Measurement model

In this work, a range sonar system with four channels is considered for the device to obtain the spatial information of objects in the environment in which the UUV is navigating. Although the range sonar system can provide only the range, the measurements for the SLAM in this work are the distance and angles between the UUV and the objects, because it is able to obtain the angle information from the relationship of the UUV position and the fixed position of the range sonar sensor. Figure 1 shows the concepts of the measurement component, distance, and angles.

**Figure 1 Coordinate system and the measurement of range and angle.**

The measurement model for the four channel range sonar system is described as follows:

$$\mathbf{z}(k+1) = \begin{bmatrix} \mathbf{z}_1(k+1) \\ \mathbf{z}_2(k+1) \\ \mathbf{z}_3(k+1) \\ \mathbf{z}_4(k+1) \end{bmatrix} + \begin{bmatrix} \mathbf{w}_1(k+1) \\ \mathbf{w}_2(k+1) \\ \mathbf{w}_3(k+1) \\ \mathbf{w}_4(k+1) \end{bmatrix}. \quad (5)$$

The subscript in (5) denotes the corresponding direction in the range sonar system. The orders of direction for the range sonar are front, starboard, port, and downward. The measurement model for single objects detected by the  $i^{th}$  range sonar at time  $k+1$  is described as follows:

$$\mathbf{z}_i = \begin{bmatrix} r_i(k+1) \\ \alpha_i(k+1) \\ \beta_i(k+1) \end{bmatrix} + \mathbf{w}(k+1). \quad (6)$$

In (6),  $r_i(k+1)$  is the distance,  $\alpha_i(k+1)$  is the angle rotated from the  $z$  axis,  $\beta_i(k+1)$  is the angle rotated from the  $y$  axis, and  $\mathbf{w}(k+1)$  represents the measurement noises of the sonar, which are assumed to have a zero mean white Gaussian noise with the covariance dependent on the sonar specifications.

### C. SLAM formulation

The first step of the proposed scheme is the calculation of sigma points, which is the essential component of UKF. The prediction at time  $k+1$  for the state system vector described in (3) is performed using the calculated sigma points through the weight sum method of the UKF. The prediction of the measurement is performed in the same manner as the prediction of the system state vector. Following the prediction, the measurement is made. After the measurement step, the detection of new objects is decided by 'data association', which determines whether the measurements obtained by the sonar are to be labeled as new objects or as existing objects already registered on the map. Data

association is one of the most important SLAM factors for practical SLAM implementation because one incorrect data association can introduce divergence into the map estimate. Even though data association is an important problem in SLAM, in this work, the nearest neighborhood standard filter (NNSF) (Bar-Shalom and Forman, 1988) is used as the data association method instead of developing a new data association algorithm because the purpose of this paper is the implementation the SLAM based UKF into small UUVs. Measurements that do not correspond to existing objects through data association based on NNSF are considered as new objects and are registered. Whenever a new object is detected, it is added to the existing system state vector and covariance matrix using the stochastic map.

As the operation time of the UUV increases, the sizes of the system state vector and its covariance matrix increase in identical proportions as a number of newly detected objects are added; the computational burden grows as  $O(M^2)$ , where  $M$  is the size of the system state vector. This computational burden can become very large as the operation time increases. Therefore, it is necessary to adopt a method to reduce the computational burden. Previous studies have provided several alternatives that can reduce the computational burden (Newman 1999; Williams *et al.* 2002). In this paper, the local submap method (Kim, 2004) is adopted. In the local submap method, the environment in which the UUV is navigating is divided into several local submaps, and the full covariance method is used to estimate the positions of the UUV and objects in a single submap.

### Simulations in towing tank condition

#### A. Conditions

In order to verify the proposed method, several simulations were performed. It was assumed that the UUV is navigating in a water tank with a length of 120 m, breadth of 8 m, and depth of 3.5 m, while detecting the walls and floor of the tank and extra objects lying within the tank. Four sets of simulation conditions were chosen as shown in Table 1. Sets 1 and 2 are cases for two degrees of freedom motion in which the yaw varies with small and large angular motions; Sets 3 and 4 are those for three degrees of freedom motion in which the yaw and pitch vary. In Set 3, the heading and pitch change sequentially, whereas in Set 4 both angles change simultaneously. The extra objects are assumed to be located regularly in the tank. Three channels (forward, left, and right) of the range sonar were used for the 2 degrees of freedom motion and an extra channel (downward) was used for the 3 degrees of freedom motion. A comparison between the proposed method and EKF based SLAM was performed to verify the function for UKF-SLAM, which is proposed in this paper under nonlinear conditions. The basic parameters of the EKF are shown in Table 2. The standard deviation of acceleration, heading, and pitch were decided considering the specification of the SNUUV I under development.

**Table 1. Simulation conditions**

No.	UUV Velocity	No. of channels	No. of extra objects	UUV angle variation
1	0.1, 0.3, 0.5 m/s	3 ch.	4-8 objects	-5 ~ 5°
2	0.1, 0.3, 0.5 m/s	3 ch.	4-8 objects	-10 ~ 10°
3	0.1, 0.3 m/s	4 ch.	0	-10 ~ 10° ( respectively change of heading and pitch)
4	0.1, 0.3 m/s	4 ch.	0	-10 ~ 10° (concurrent change of heading and pitch)

**Table 2. Basic parameters of EKF**

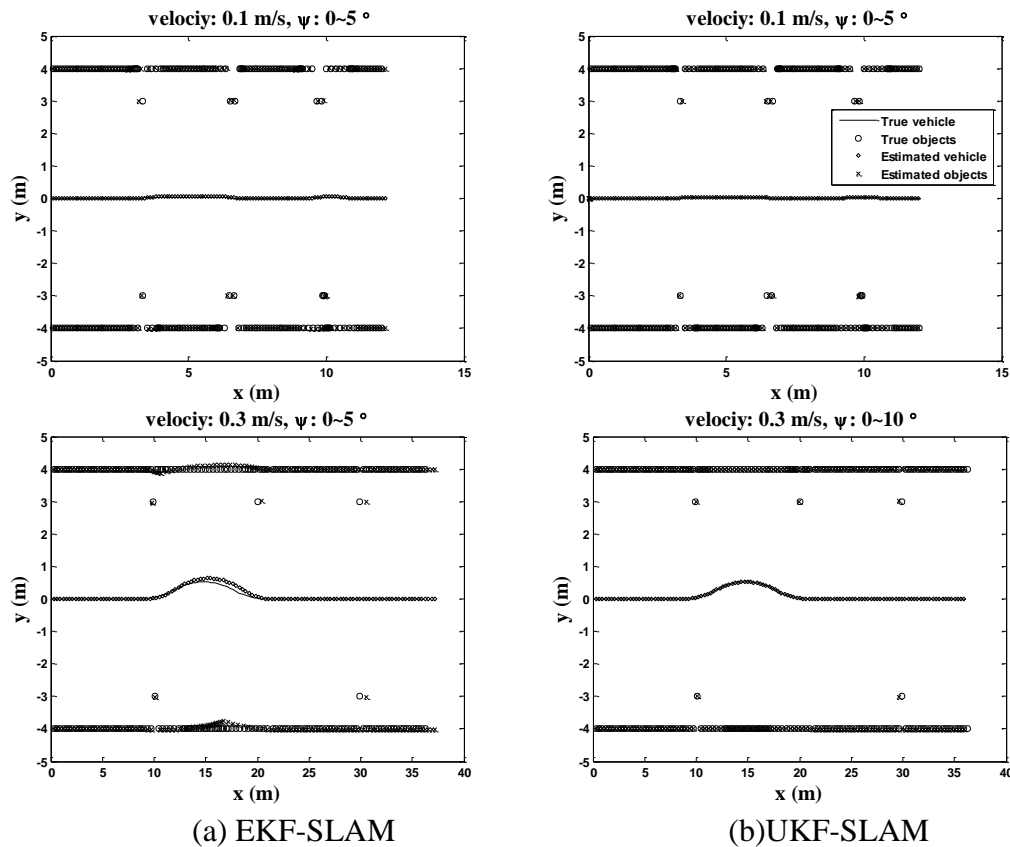
Parameters	Value
Variance of vehicle acceleration	0.01 m/s <sup>2</sup>
Variance of vehicle angles	1°
Variance of object position	1 m
Variance of range	1 m
Variance of angles	5°

## B. Simulation results

Figure 2 shows several representative results for the 2 degrees of freedom motion simulation. The origin of the 2 dimensional map is the UUV starting point. The true positions of the UUV and objects (continuous walls and five isolated targets) are designated by a solid line (-) and circles (○), respectively, while the estimated positions of the vehicle and objects are shown using crosses (+) and x marks (x), respectively. The left and right column figures are the EKF-SLAM and UKF-SLAM results, respectively. From Fig. 2, when the nonlinearity of the UUV motion is weak (when the UUV velocity is slow and yaw variance is small), both methods show little error in the mapping and localization results; however, when the UUV moves quickly or the yaw varies with large angles, the UKF-SLAM provides more accurate mapping and localization results than the EKF-SLAM. This verifies that the method proposed in this paper is suitable for the nonlinear

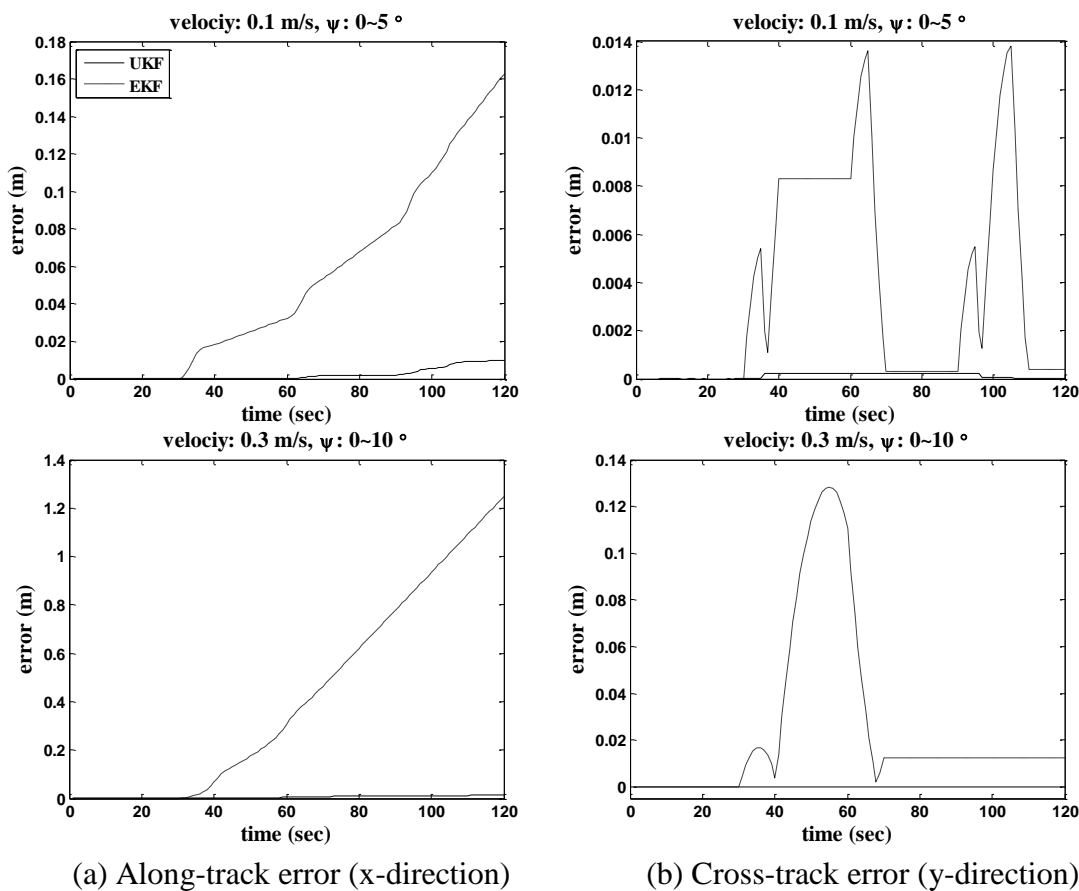
motions of UUVs. Figure 3 shows the UUV location estimation errors, i.e. the difference between the solid line and the crosses in Fig. 2. The solid line is the error from the UKF-SLAM and the dashed line is that of the EKF-SLAM. The EKF error increases once the heading angle begins to change at time 30 sec; that is, the nonlinearity occurred in the state transition as predicted in the theory.

**Figure 2. Simulation results of (a) EKF-SLAM and (b) UKF-SLAM for 2D motion depending on the heading angle changes and vehicle velocity.**





**Figure 3. . Comparison of estimation errors of the UUV location using EKF-SLAM and UKF-SLAM in the 2D motion simulation; (a) along-track and (b) cross-track directions.**



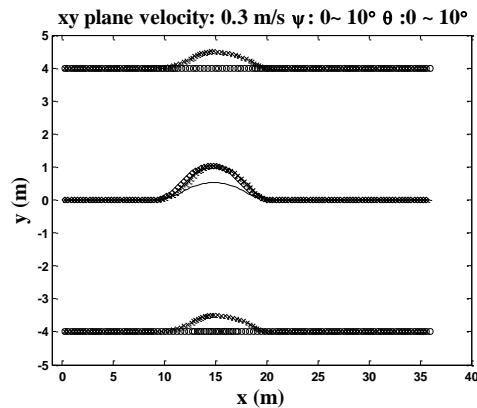
The root mean square error (RMSE) of the EKF-SLAM is more than twice that of the proposed method. From Fig. 3, the RMSEs of the proposed method in the  $x$  and  $y$  directions are 0.233 m and 0.004 m in the upper section of Fig. 3, and 0.191 m and 0.004 m in the lower section of Fig. 3; however, the RMSEs of EKF-SLAM are 0.436 m and 0.014 m in the upper section of Fig. 3, and 0.428 m and 0.025 m in the lower section of Fig. 3.

The simulation results of the three degrees of freedom motion are depicted in Fig. 4. The difference in performances of both methods is seen in the 3D motion simulation, where the nonlinearity is generally stronger. Figure 4(a) and 4(b) show the EKF-SLAM and UKF-SLAM simulation results for the Set 3 motion from Table 1 and Figs. 4(c) and 4(d) present the both method simulation results for the Set 4 motion from Table 1. The upper section of the Figs. 4(a), 4(b), 4(c) and 4(d) is the horizontal plane ( $x$ - $y$ ) results and the lower is the vertical plane ( $x$ - $z$ ) result. The same symbols in Fig. 2 are used to describe the true positions of the UUV and objects, the estimated positions of the vehicle and objects in Fig. 5. Figs. 4(a) and 4(b) prove the UKF-SLAM can produce the more accurate mapping and localization results than the EKF-SLAM when the heading and pitch vary simultaneously. The sequential motion results shown in Figs. 4(c) and 4(d) also show prove the UKF-SLAM is more suitable for nonlinear case than EKF-SLAM. Fig. 5 shows that the UKF-SLAM provides more

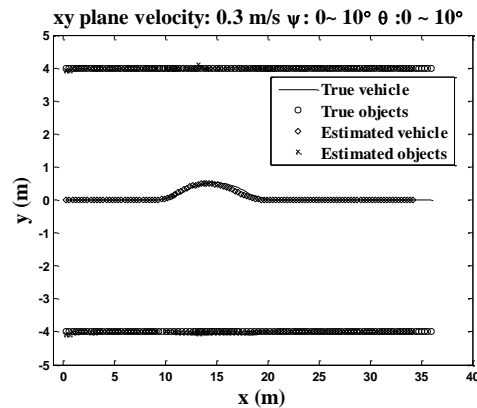


accurate mapping and localization results than the EKL-SLAM when the UUV motion is the three degrees of freedom motion. The simulation results clearly prove that the proposed method has better performance than that of EKF-SLAM when nonlinearity is strong.

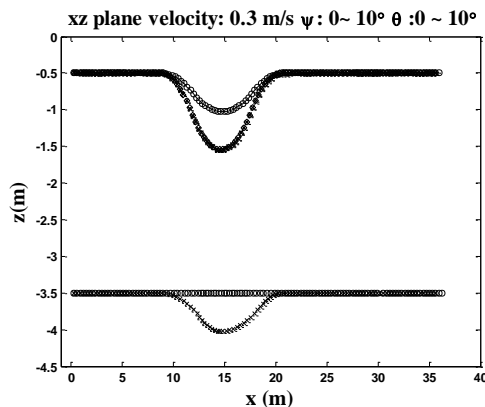
**Figure 4. Simulation results of (a) EKF-SLAM and (b) UKF- SLAM for 3D motion depending on the heading angle changes and vehicle velocity.**



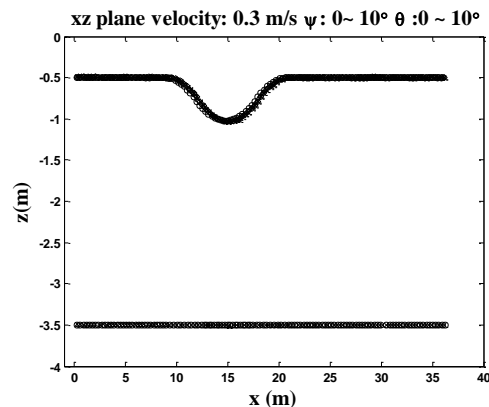
(a) EKF-SLAM concurrent



(b) UKF-SLAM concurrent



(c) EKF-SLAM sequential



(d) UKF-SLAM sequential

## Conclusion

This paper presents a SLAM method that relies solely on range sonar data, which is suitable for a small UUV with a limited payload and computing power. The method uses an unscented Kalman filter to estimate the system state vector with multiple objects using a nonlinear system equation instead of a linearized equation when the UUV navigates in a three dimensional space. It also adopts the nearest neighborhood standard filter for data association and the local submap method to reduce the computational power. The proposed method was tested through computer simulations under various conditions of varying the vehicle velocity, ranges, heading angles, and pitch angles. The simulation results showed that the proposed method produces better localization of the vehicle state

and objects mapping in both two dimensional and three dimensional motions than that of the EKF-SLAM. Future works will investigate the feasibility of integrating SLAM into the total navigation system of real UUVs where it will function as a module that provides information about the surrounding environment and to experiment with the UUV and the proposed SLAM method in a fully autonomous navigation mode in the towing tank.

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